

The parameter values are:

	$u_1$	$u_2$	$u_3$	$x$	$z$
$Ba_3(PO_4)_2$	$0.208 \pm 0.004$	$0.412 \pm 0.008$	0.337	0.285	0.742
$Sr_3(PO_4)_2$	$0.208 \pm 0.004$	$0.412 \pm 0.008$	0.333	0.279	0.753

Table 2 lists calculated and observed intensities for  $Ba_3(PO_4)_2$ . The former were obtained using the formula

$$I \propto |F|^2 p \frac{1 + \cos^2 2\theta}{\sin^2 \theta \cos \theta},$$

where  $p$  is the permutation factor. The observed intensities were measured using the Norelco Spectrometer.

### Discussion of the structure

The tetrahedral configuration of four oxygen atoms (one  $O_I$  and three  $O_{II}$ ) about phosphorus with

$$P-O_I = P-O_{II} = 1.56 \text{ \AA.}$$

was assumed. The configuration of oxygen atoms about barium and strontium atoms is as follows:

$$\begin{aligned} Ba_I-6 O_I &= 3.23 \text{ \AA.}, & Ba_I-6 O_{II} &= 2.80 \text{ \AA.}, \\ Ba_{II}-1 O_I &= 2.71 \text{ \AA.}, & Ba_{II}-3 O_{II} &= 2.80 \text{ \AA.}, \\ Ba_{II}-6 O_{II} &= 2.83 \text{ \AA.}; \\ Sr_I-6 O_I &= 3.10 \text{ \AA.}, & Sr_I-6 O_{II} &= 2.63 \text{ \AA.}, \\ Sr_{II}-1 O_I &= 2.48 \text{ \AA.}, & Sr_{II}-3 O_{II} &= 2.62 \text{ \AA.}, \\ Sr_{II}-6 O_{II} &= 2.72 \text{ \AA.} \end{aligned}$$

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## Crystal Chemical Studies of the 5f-Series of Elements. I. New Structure Types

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(Received 14 August 1948)

The paper gives brief descriptions of new structure types observed for simple compounds of the 5f-series of elements and of related elements.

### Introduction

In the course of the last five years the writer has determined the crystal structures of a number of compounds of thorium, of uranium, of the transuranic elements, and of the rare elements actinium and protactinium. The work was started in the Manhattan Project and has been continued in the Argonne National Laboratory after the war.

The crystal-structure studies of compounds of the new and rare elements were undertaken for the main purpose of determining the chemical identity of the various micro-preparations, so that the basic chemistry of these elements could be deduced at a time when only microgram amounts were available. In most instances it became necessary to carry out at least a partial

Thus barium or strontium atoms of the first kind show co-ordination number twelve, barium and strontium atoms of the second kind co-ordination number ten. The total strength of the bonds ending on  $O_I$  is 1.95 and on  $O_{II}$  2.02.

The observed mean interionic distances and those calculated from ionic radii (Zachariasen, 1931) agree reasonably well as shown below:

	Observed	Calculated
$Ba_I-O$	3.01 A.	2.96 A.
$Ba_{II}-O$	2.81	2.90
$Ba-O$ mean	2.88	2.92
$Sr_I-O$	2.86	2.78
$Sr_{II}-O$	2.67	2.72
$Sr-O$ mean	2.73	2.74

In view of the close crystal chemical similarity of lead to strontium and barium it was attempted to prepare the isostructural lead compound. These efforts were unsuccessful.

The writer wishes to thank Miss Anne Plettinger for having taken the X-ray diffraction patterns, and Mr H. B. Evans for having made the chemical preparations, the chemical analyses and the direct density determinations.

### References

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crystal-structure determination before the chemical identity of the substance could be ascertained.

This is the first of a series of articles bearing the general title 'Crystal Chemical Studies of the 5f-Series of Elements' in which the results of these investigations will be reported. Most of the articles will describe the crystal-structure determination of groups of compounds or of individual compounds. Other articles in the series will contain general discussions of the crystal chemistry of the 5f-series of elements. A few of the articles will, like the present one, summarize crystal-structure results which have been obtained.

All the structures described in this article were deduced from X-ray diffraction patterns of crystal powders. Only in two instances,  $PuCl_3$  and  $Na_3UF_7$ ,

did single crystals subsequently become available. A number of the structures contain light atoms such as oxygen and fluorine. In some cases it was possible to deduce the positions of the light atoms solely from intensity calculations, in other cases it was necessary to make use of considerations based upon interatomic distances.

The information given about the various structure types include the unit-cell dimensions, the number of stoichiometric molecules per unit cell ( $n$ ), the space group, the atomic positions and the interatomic distances. In giving the atomic positions the nomenclature of the *International Tables for the Determination of Crystal Structures* is used. A statement such as U-9 Cl=2.96 A. implies that each uranium atom is bonded to nine chlorine atoms at a mean distance of 2.96 A.

#### Structure type: UCl<sub>3</sub>

Hexagonal;  $n=2$ ; space group:  $C6_3/m-C_{6h}^2$ .

2 U in 2(*a*).

6 Cl in 6(*h*), with  $x=0.375$ ,  $y=0.292$ .

U-9 Cl=2.96 A.

The unit-cell dimensions are:

	$a_1$ (kX.)	$a_3$ (kX.)
AcCl <sub>3</sub>	7.62 ± 0.02	4.55 ± 0.02
UCl <sub>3</sub>	7.428 ± 0.003	4.312 ± 0.003
NpCl <sub>3</sub>	7.405 ± 0.010	4.273 ± 0.005
PuCl <sub>3</sub>	7.380 ± 0.001	4.238 ± 0.001
AmCl <sub>3</sub>	7.37 ± 0.01	4.24 ± 0.01
LaCl <sub>3</sub>	7.468 ± 0.003	4.366 ± 0.003
CeCl <sub>3</sub>	7.436 ± 0.004	4.304 ± 0.004
PrCl <sub>3</sub>	7.41 ± 0.01	4.25 ± 0.01
NdCl <sub>3</sub>	7.381 ± 0.004	4.231 ± 0.003
AcBr <sub>3</sub>	8.06 ± 0.04	4.68 ± 0.02
UBr <sub>3</sub>	7.926 ± 0.002	4.432 ± 0.002
$\alpha$ -NpBr <sub>3</sub>	7.917 ± 0.005	4.382 ± 0.005
LaBr <sub>3</sub>	7.951 ± 0.003	4.501 ± 0.003
CeBr <sub>3</sub>	7.936 ± 0.003	4.435 ± 0.003
PrBr <sub>3</sub>	7.92 ± 0.01	4.38 ± 0.01
La(OH) <sub>3</sub>	6.510 ± 0.005	3.843 ± 0.005
Pr(OH) <sub>3</sub>	6.47 ± 0.03	3.76 ± 0.03
Nd(OH) <sub>3</sub>	6.42 ± 0.02	3.74 ± 0.02

#### Structure type: PuBr<sub>3</sub>

Orthorhombic;  $n=4$ ; space group:  $Ccmm-D_{2h}^{17}$ .

4 Pu in 4(*c*), with  $x=0.25$ .

4 Br<sub>I</sub> in 4(*c*), with  $x=-0.07$ .

8 Br<sub>II</sub> in 8(*f*), with  $x=0.36$ ,  $z=-0.05$ .

Pu-8 Br=3.08 A.

This is a layer structure with layers normal to  $a_1$ .

The unit-cell dimensions are:

	$a_1$ (kX.)	$a_2$ (kX.)	$a_3$ (kX.)
$\beta$ -NpBr <sub>3</sub>	12.65 ± 0.05	4.11 ± 0.03	9.15 ± 0.04
PuBr <sub>3</sub>	12.62 ± 0.05	4.09 ± 0.03	9.13 ± 0.04
AmBr <sub>3</sub>	12.6 ± 0.1	4.10 ± 0.04	9.10 ± 0.05
NdBr <sub>3</sub>	12.63 ± 0.05	4.10 ± 0.03	9.15 ± 0.04
SmBr <sub>3</sub>	12.62 ± 0.05	4.03 ± 0.03	9.06 ± 0.04
UI <sub>3</sub>	13.98 ± 0.06	4.31 ± 0.03	9.99 ± 0.05
NpI <sub>3</sub>	14.00 ± 0.06	4.29 ± 0.03	9.93 ± 0.05
PuI <sub>3</sub>	14.00 ± 0.06	4.29 ± 0.03	9.90 ± 0.05
AmI <sub>3</sub>	14.0 ± 0.1	4.30 ± 0.05	9.9 ± 0.1
LaI <sub>3</sub>	14.1 ± 0.1	4.33 ± 0.05	10.05 ± 0.10

#### Structure type: Ce<sub>2</sub>S<sub>3</sub>

Cubic;  $n=16/3$ ; space group:  $I\bar{4}3d-T_2^6$ .

10 $\frac{2}{3}$ -12 Ce in 12(*a*).

16 S in 16(*c*), with  $x=0.083$ .

Ce-8 S=2.98 A.

The ideal composition is Ce<sub>3</sub>S<sub>4</sub> with  $n=4$ .

The unit-cell dimensions are:

	$a$ (kX.)
Ac <sub>2</sub> S <sub>3</sub>	8.97 ± 0.01
Pu <sub>2</sub> S <sub>3</sub>	8.4373 ± 0.0005
Am <sub>2</sub> S <sub>3</sub>	8.428 ± 0.002
La <sub>2</sub> S <sub>3</sub>	8.706 ± 0.001
Ce <sub>2</sub> S <sub>3</sub>	8.6173 ± 0.0005
Ce <sub>3</sub> S <sub>4</sub>	8.6076 ± 0.0005

#### Structure type: $\beta_2$ -Na<sub>2</sub>ThF<sub>6</sub>

Hexagonal;  $n=1$ ; space group:  $C32-D_3^2$ .

2 Na in 2(*d*), with  $z=0.385$ .

1 Th in 1(*a*).

3 F in 3(*e*), with  $x=0.600$ .

3 F in 3(*f*), with  $x=0.250$ .

Na-6 F=2.33 A., Th-9 F=2.41 A.

For the isomorphous compounds NaPuF<sub>4</sub>, NaLaF<sub>4</sub>, NaCeF<sub>4</sub>,  $n=\frac{3}{2}$  with 1.5 Na + 0.5 Pu in 2(*d*) and 1 Pu in 1(*a*).

The unit-cell dimensions are:

	$a_1$ (kX.)	$a_3$ (kX.)
$\beta_2$ -Na <sub>2</sub> ThF <sub>6</sub>	5.977 ± 0.005	3.827 ± 0.005
$\beta_2$ -K <sub>2</sub> UF <sub>6</sub>	6.53 ± 0.02	4.04 ± 0.01
$\beta_2$ -Na <sub>2</sub> UF <sub>6</sub>	5.94 ± 0.01	3.74 ± 0.01
NaPuF <sub>4</sub>	6.117 ± 0.006	3.746 ± 0.004
NaLaF <sub>4</sub>	6.167 ± 0.001	3.819 ± 0.002
NaCeF <sub>4</sub>	6.140 ± 0.001	3.770 ± 0.001

#### Structure type: $\beta_1$ -K<sub>2</sub>UF<sub>6</sub>

Hexagonal;  $n=1$ ; space group:  $C\bar{6}2m-D_{3h}^3$ .

2 K in 2(*d*).

1 U in 1(*a*).

3 F in 3(*f*), with  $x=0.640$ .

3 F in 3(*g*), with  $x=0.220$ .

K-9 F=2.73 A., U-9 F=2.36 A.

$n=\frac{3}{2}$  for isomorphous compounds KXF<sub>4</sub> with 1.5 K + 0.5 X in 2(*d*) and 1 X in 1(*a*).

The unit-cell dimensions are:

	$a_1$ (kX.)	$a_3$ (kX.)
$\beta_1$ -K <sub>2</sub> ThF <sub>6</sub>	6.565 ± 0.002	3.815 ± 0.001
$\beta_1$ -K <sub>2</sub> UF <sub>6</sub>	6.53 ± 0.01	3.77 ± 0.01
$\beta_1$ -KLaF <sub>4</sub>	6.524 ± 0.001	3.791 ± 0.001
$\beta_1$ -KCeF <sub>4</sub>	6.496 ± 0.001	3.750 ± 0.001

**Structure type: Ce<sub>2</sub>O<sub>2</sub>S**Hexagonal;  $n=1$ ; space group:  $C\bar{3}m-D_{3d}^3$ .2 Ce in 2(*d*), with  $z=0.208$ .1 S in 1(*b*).2 O in 2(*d*), with  $z=-0.137$ .

Ce-3 S = 3.04 Å., Ce-4 O = 2.36 Å.

The structure is closely related to that of La<sub>2</sub>O<sub>3</sub>.

The unit-cell dimensions are:

	$a_1$ (kX.)	$a_3$ (kX.)
Pu <sub>2</sub> O <sub>2</sub> S	3.919 ± 0.003	6.755 ± 0.010
La <sub>2</sub> O <sub>2</sub> S	4.03 ± 0.02	6.88 ± 0.04
Ce <sub>2</sub> O <sub>2</sub> S	4.00 ± 0.01	6.82 ± 0.03

**Structure type: Ca(UO<sub>2</sub>)O<sub>2</sub>**Rhombohedral;  $n=1$ ; space group:  $R\bar{3}m-D_{3d}^5$ .1 Ca in 1(*b*).1 U in 1(*a*).2 O<sub>I</sub> in 2(*c*), with  $x=0.109$ .2 O<sub>II</sub> in 2(*c*), with  $x=0.361$ .Ca-8 O = 2.45 Å., U-2 O<sub>I</sub> = 1.91 Å., U-6 O<sub>II</sub> = 2.29 Å.

The structure contains linear uranyl groups O-U-O.

The unit-cell dimensions are:

	$a$ (kX.)	$\alpha$
CaUO <sub>4</sub>	6.254 ± 0.001	36° 2' ± 1'
SrUO <sub>4</sub>	6.53 ± 0.03	35° 32' ± 20'

**Structure type: UO<sub>2</sub>F<sub>2</sub>**Rhombohedral;  $n=1$ ; space group:  $R\bar{3}m-D_{3d}^5$ . $a=5.764 \pm 0.001$  kX.,  $\alpha=42^\circ 43' \pm 3'$ .1 U in 1(*a*).2 O in 2(*c*), with  $x=0.122$ .2 F in 2(*c*), with  $x=0.294$ .

U-2 O = 1.91 Å. (assumed), U-6 F = 2.50 Å.

This is a typical layer structure. There is stacking disorder.

**Structure type: U<sub>2</sub>F<sub>9</sub>**Cubic;  $n=4$ ; space group:  $I\bar{4}3m-T_d^3$ .8 U in 8(*c*), with  $x=0.187$ .12 F in 12(*e*), with  $x=0.225$ .24 F in 24(*g*), with  $x=0.20$ ,  $z=0.46$ .

U-9 F = 2.31 Å.

In the isomorphous compound NaTh<sub>2</sub>F<sub>9</sub>, the six holes 6(*b*) are occupied by four sodium atoms.

The unit-cell dimensions are:

	$a$ (kX.)
U <sub>2</sub> F <sub>9</sub>	8.4545 ± 0.0005
NaTh <sub>2</sub> F <sub>9</sub>	8.705 ± 0.001

**Structure type: α-UF<sub>6</sub>**Tetragonal;  $n=2$ ; space group:  $I4/m-C_{4h}^5$ . $a_1=6.512 \pm 0.001$  kX.,  $a_3=4.463 \pm 0.001$  kX.2 U in 2(*a*).2 F<sub>I</sub> in 2(*b*).8 F<sub>II</sub> in 8(*h*), with  $x=0.32$ ,  $y=0.11$ .U-2 F<sub>I</sub> = 2.23 Å., U-4 F<sub>II</sub> = 2.20 Å.There are strings of UF<sub>6</sub> octahedra along  $a_3$ .**Structure type: β-UF<sub>6</sub>**Tetragonal;  $n=8$ ; space group:  $I\bar{4}2d-D_{2d}^{12}$ . $a_1=11.450 \pm 0.002$  kX.,  $a_3=5.198 \pm 0.001$  kX.8 U in 8(*d*), with  $x=0.083$ .8 F<sub>I</sub> in 8(*d*), with  $x=0.278$ .16 F<sub>II</sub> in 16(*e*), with  $x=0.167$ ,  $y=0.083$ ,  $z=0$ .16 F<sub>III</sub> in 16(*e*), with  $x=0.042$ ,  $y=0.125$ ,  $z=0.445$ .

U-7 F = 2.23 Å.

**Structure type: γ-Na<sub>2</sub>UF<sub>6</sub>**Orthorhombic;  $n=2$ ; space group:  $Immm-D_{2h}^{25}$ . $a_1=5.54 \pm 0.01$  kX.,  $a_2=4.01 \pm 0.01$  kX., $a_3=11.67 \pm 0.02$  kX.2 U in 2(*a*).4 Na in 4(*i*), with  $z=\frac{1}{2}$ .4 F<sub>I</sub> in 4(*f*), with  $x=\frac{1}{4}$ .8 F<sub>II</sub> in 8(*m*), with  $x=\frac{1}{4}$ ,  $z=\frac{1}{8}$ .

Na-8 F = 2.38 Å., U-8 F = 2.38 Å.

**Structure type: Na<sub>3</sub>UF<sub>7</sub>**Tetragonal;  $n=2$ ; space group:  $I4/mmm-D_{4h}^{17}$ . $a_1=5.448 \pm 0.007$  kX.,  $a_3=10.896 \pm 0.014$  kX.2 U in 2(*a*).2 Na<sub>I</sub> in 2(*b*).4 Na<sub>II</sub> in 4(*d*).14 F in 16(*m*), with  $x=\frac{1}{4}$ ,  $z=\frac{1}{8}$ .

Na-7 F = 2.36 Å., U-7 F = 2.36 Å.

The structure is closely related to that of fluorite.

**Structure type: UCl<sub>6</sub>**Hexagonal;  $n=3$ ; space group:  $C\bar{3}m-D_{3d}^3$ . $a_1=10.95 \pm 0.02$  kX.,  $a_3=6.03 \pm 0.01$  kX.1 U<sub>I</sub> in 1(*a*).2 U<sub>II</sub> in 2(*d*), with  $z=\frac{1}{2}$ .6 Cl<sub>I</sub> in 6(*i*), with  $x=0.10$ ,  $z=\frac{1}{4}$ .6 Cl<sub>II</sub> in 6(*i*), with  $x=0.43$ ,  $z=\frac{1}{4}$ .6 Cl<sub>III</sub> in 6(*i*), with  $x=0.77$ ,  $z=\frac{1}{4}$ .

U-6 Cl = 2.42 Å.

This is a typical molecular structure.

**Structure type:  $U_3Si_3$** 

Tetragonal;  $n = 2$ ; space group:  $P4/mbm-D_{4h}^5$ .  
 $a_1 = 7.3151 \pm 0.0004$  kX.,  $a_3 = 3.8925 \pm 0.0005$  kX.  
 $2 U_I$  in  $2(a)$ .  
 $4 U_{II}$  in  $4(h)$ , with  $x = 0.181$ .  
 $4 Si$  in  $4(g)$ , with  $x = 0.389$ .  
 $U_I-4 Si = 2.96$  A.,  $U_I-8 U_{II} = 3.32$  A.,  
 $U_{II}-6 Si = 2.92$  A.,  $U_{II}-4 U_I = 3.32$  A.,  
 $Si-1 Si = 2.30$  A.  
 The structure contains pairs of Si atoms.

**Structure type:  $U_3Si$** 

Tetragonal;  $n = 4$ ; space group:  $I4/mcm-D_{4h}^{18}$ .  
 $a_1 = 6.017 \pm 0.002$  kX.,  $a_3 = 8.679 \pm 0.003$  kX.  
 $4 U_I$  in  $4(a)$ .  
 $8 U_{II}$  in  $8(h)$ , with  $x = 0.231$ .  
 $4 Si$  in  $4(b)$ .  
 $U_I-4 Si = 3.01$  A.,  $U_I-8 U_{II} = 3.04$  A.,  
 $U_{II}-2 Si = 2.92$  A.,  $U_{II}-2 Si = 3.17$  A.,  
 $U_{II}-4 U_{II} = 3.02$  A.,  $U_{II}-4 U_I = 3.04$  A.  
 The structure is closely related to that of  $AuCu_3$ .

**Structure type:  $\alpha-UO_3$** 

Hexagonal;  $n = 1$ ; space group:  $C3m-D_{3d}^3$ .  
 $a_1 = 3.963 \pm 0.004$  kX.,  $a_3 = 4.160 \pm 0.008$  kX.  
 $1 U$  in  $1(a)$ .  
 $1 O_I$  in  $1(b)$ .

$2 O_{II}$  in  $2(d)$ , with  $z = 0.17$ .

$U-2 O_I = 2.08$  A.,  $U-6 O_{II} = 2.39$  A.

There are endless chains  $-O_I-U-O_I-U-$  along  $a_3$ .

The orthorhombic  $U_3O_8$  structure is closely related.

**Remarks**

The compounds of actinium, neptunium, plutonium and americium referred to in this paper were first prepared by various investigators as follows:

Sherman Fried and F. Hagemann:  $AcCl_3$ ,  $AcBr_3$ ,  $Ac_2S_3$ .

Sherman Fried:  $AmCl_3$ ,  $\alpha-NpBr_3$ ,  $AmBr_3$ ,  $NpI_3$ ,  $AmI_3$ ,  $Am_2S_3$ .

Sherman Fried and N. R. Davidson:  $NpCl_3$ .

I. Sheft:  $\beta-NpBr_3$ .

F. Hagemann:  $PuCl_3$ ,  $PuI_3$ .

N. R. Davidson:  $Pu_2O_2S$ ,  $Pu_2S_3$ .

E. K. Hyde:  $PuBr_3$ .

H. L. Baumbach:  $NaPuF_4$ .

With the single exception of  $PuBr_3$  all of the compounds listed above were first identified by the writer through interpretation of the X-ray diffraction patterns.

Miss Anne Plettinger gave valuable aid by taking all of the powder diffraction patterns.

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## Crystal Chemical Studies of the 5f-Series of Elements.

### II. The Crystal Structure of $Cs_2PuCl_6$

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(Received 22 July 1948)

$Cs_2PuCl_6$  is trigonal and has the  $K_2GeF_6$ -type of structure. The unit-cell dimensions are:

$$a_1 = 7.43 \pm 0.01 \text{ kX.}, \quad a_3 = 6.03 \pm 0.01 \text{ kX.},$$

giving a calculated density of  $\rho = 4.10 \text{ g.cm}^{-3}$ . Plutonium is bonded to six chlorine atoms at the corners of an octahedron with  $Pu-Cl = 2.62$  A. Cesium is bonded to twelve chlorine atoms with  $Cs-Cl = 3.71$  A.

The compound  $Cs_2PuCl_6$  was first prepared by Herbert H. Anderson,\* who also established the identity of the substance by direct chemical analysis. The results given below were obtained using a micro-sample of the original preparation kindly lent to the writer by Dr Anderson.

The sample consisted of a small amount of powdered material in a sealed, thin-walled glass capillary. The powder diffraction photographs were taken with Cu K radiation filtered through nickel foil.

\* Report ANL-4056 of the Argonne National Laboratory.

Table 1 gives a portion of the diffraction data (up to  $\sin^2 \theta = 0.310$ ). The observed sine squares correspond to a hexagonal unit cell with dimensions

$$a_1 = 7.43 \pm 0.01 \text{ kX.}, \quad a_3 = 6.03 \pm 0.01 \text{ kX.}$$

In this cell there is room for but one molecule  $Cs_2PuCl_6$ , giving a calculated density  $\rho = 4.10 \text{ g.cm}^{-3}$ .

Reflections  $H_1H_20$  are missing if  $H_1 - H_2 = 3n \pm 1$ . Reflections  $H_1H_2H_3$  for which  $H_1 - H_2 = 3n$  are strong when  $H_3 = 0$  or 4, weak when  $H_3 = 1$  or 3, and missing when  $H_3 = 2$ . These observations require the cesium positions to be  $\pm (\frac{2}{3}, \frac{1}{3}, u)$  with  $u \approx \frac{1}{4}$ .